



Examination Answer Books

12 Pages

Instructions to Candidates

1. Please give the information requested in the boxes below.
2. Enter your name in the space provided to the right, fold over and seal down (using the label provided) to hide your name.
3. The answers must be legibly written. The Examiners can either ignore illegible script or have it typed and the expense of typing charged to the candidate.
4. Write your answers in ink.
5. Begin each answer on a fresh page. Do all rough work in the answer book and cross it through.
6. No part of this book is to be torn out; it must be handed in complete.
7. If more books than one are used, fasten them together using the tags available from the invigilator(s).
8. Every book must be handed in. In no circumstances may answer books, used or unused, be taken out of the examination venue.

Complete, fold and seal
(see note 2 below)

SURNAME: Morgan

FORENAME(S): Matthew James

1	Student Number	MOR17833826
2	Title of Examination Paper	Mathematics test 1
3	Module Code	GOEN4001
4	Date and Time of Examination	Monday, 23rd Jan 23 13:30
5	Examination Venue	ward 2, Gower College
6	Seat Number	6
7	Number of Answer Books handed in	

List the numbers of the questions you have attempted	Office Use
Q1 a	22
b	6
c	2
d	2
Q2 a	1
b	0
c	2
d	0
e	4
Q3 a	6
b	4
c	0
d	1
Total	50%

50%

1)

$$i) y = 6x^4 + 5x^3 + 3x^2 + 6x + 7$$

$$dy = 24x^3 + 15x^2 + 6x + 6$$

2

$$ii) y = \sin 5x + 5 \cos 4x + 7 \tan 3x$$

$$y = 5 \cos 5x + 20 \sin 4x +$$

$$dy = 5 \cos 5x - 20 \sin 4x + 21 \sec^2 3x$$

2

$$iii) y = 3 + \frac{1}{x^5} + \sqrt[4]{x}$$

$$y = x^{-5} + x^{\frac{1}{4}}$$

$$dy = -5x^{-6} + \frac{1}{4}x^{-\frac{3}{4}}$$

2

$$iv) y = \sin 2x e^{5x}$$

$$u = \sin 2x$$

$$\frac{du}{dx} = 2 \cos 2x$$

$$v = e^{5x}$$

$$\frac{dv}{dx} = 5e^{5x}$$

$$\frac{dy}{dx}$$

$$\sin 2x (5e^{5x}) + e^{5x} (2 \cos 2x)$$

$$v) y = 15(2x^3 + 3)^4$$

$$dy = 60(2x^3 + 3)^3 \cdot 6x^2$$

3

$$vi) y = 6x \sqrt{7x^3 + 5x}$$

$$y = (7x^3 + 5x)^{\frac{1}{2}}$$

$$y = \frac{1}{2}(7x^3 + 5x)^{-\frac{1}{2}} \times ?$$

2

$$vii) y = 4x^5 \ln x$$

$$u = 4x^5 \quad \frac{du}{dx} = 20x^4$$

$$v = \ln x \quad \frac{dv}{dx} = \frac{1}{x}$$

$$\frac{dy}{dx} = 4x^5 \left(\frac{1}{x} \right) + \ln x (20x^4)$$

4

Q1a22/23

$$\text{viii)} y = \frac{4 \cos 4x}{e^{3x}}$$

$$u = 4 \cos 4x$$

$$\frac{du}{dx} = -16 \sin 4x$$

4

$$v = e^{3x}$$

$$\frac{dv}{dx} = 3e^{3x}$$

$$\frac{dy}{dx} = \frac{e^{3x}(-16 \sin 4x) - 4 \cos 4x(3e^{3x})}{(e^{3x})^2}$$

$$\text{b)} w = 4x^4 + 3x^3y^3 + 2y^2 + 25$$

$$\frac{dw}{dx} = 16x^3 + 9x^2y^3$$

$$\frac{dw}{dy} = 9x^3y^2 + 4y$$

$$\frac{d^2w}{dx^2} = 48x^2 + 18xy^3$$

$$\frac{d^2w}{dy^2} = 18x^3y + 4$$

$$\frac{d^2w}{dydx} = 48x^2 + 54xy^2$$

$$\frac{d^2w}{dxdy} = 54x^2y$$

$$\frac{d^2w}{dydx} = 16x^2 + 27x^2y^2$$

$$\frac{d^2w}{dxdy} = 27x^2y^2$$

$$\text{c)} y = 8x^2 + 6x - 15$$

$$\frac{dy}{dx} = 16x + 6$$

$$-6 = 16x \Rightarrow \frac{-6}{16} = x$$

$$x = -0.375$$

$$\frac{d^2y}{dx^2} = 16$$

$$\text{d)} y = 2 \cos 3x \quad \frac{dy}{dx} = -6 \sin 3x \quad \frac{d^2y}{dx^2} = -18 \cos 3x \quad \frac{d^3y}{dx^3} = 54 \sin 3x \quad \frac{d^4y}{dx^4} = 162 \cos 3x$$

Q1b

6/6

Q1c

2/4

Q1d

2/9

2)

a) $\frac{2x+5}{(x-2)(x+1)} = \frac{\quad}{\quad}$

Q2a
1/10

$x=2$ ✓ or $x=-1$ ✓

$A=2$ $B=-1$ ✓ 1

$= \frac{2}{x-2} + \frac{-1}{x+1}$ ✓

b) i) $18-15=3$

Q2b
0

$18+3=21$ ✗

$B \text{ to } C = 21m$

ii) $\text{Angle } A = 100^\circ$
 $\text{Angle } B = 40^\circ$
 $\text{Angle } C = 40^\circ$ ✗

c) x^2-6x+5

Q2c
2/6

$(x-2)(x-3)$ ✓ 2

$x=2$ or $x=3$ ✓

d) $y=x^2-6x+5 = ?$ 0

Q2d
0

e)

Q2e
4/7

i) $\sin x = 0.85$

58.21° ✓, 121.79° ✓ 2

ii) $\sec x = 4$

4.98° , 355.02° ✗

iii) $\tan x = -0.8$

$38.66^\circ \rightarrow 141.34^\circ, 321.34^\circ$ ✓ 2

s	a
T	c

3)

$$a) \ln x + \ln(x-2) = \ln(x+10) \quad \times \quad \underline{\underline{0}}$$

$$iv) \frac{2x-2}{3x+9} \rightarrow \frac{4}{3}$$

$$\cancel{4(3)} \quad 3x+9(4) = 2x-2(3) \quad \checkmark$$

$$4(3x+9) = 2x-2(3) \quad \checkmark$$

$$12x+36 = 2x-6 \quad \checkmark \quad \underline{\underline{3}}$$

$$6x+36 = -6$$

$$6x = -42 \quad \checkmark$$

$$x = \frac{-42}{6} \quad \checkmark$$

$$x = -7 \quad \checkmark$$

$$v) \frac{(x+4)}{9} \times \frac{(2x-1)}{7} = 12 \quad \checkmark$$

$$7(x+4) + 9(2x-1) = 756 \quad \checkmark$$

$$7x+28+18x-9 = 756 \quad \checkmark \quad \underline{\underline{3}}$$

$$25x+19 = 756$$

$$25x = 737 \quad \checkmark$$

$$x = \frac{737}{25} \quad \checkmark$$

$$x = 29.48 \quad \checkmark$$

b)

$$ii) q^2-81$$

$$(q+9)(q-9) \quad \checkmark \quad \checkmark \quad \underline{\underline{2}}$$

$$i) z^2-9z+14$$

$$(z-7)(z-2) \quad \checkmark \quad \checkmark \quad \underline{\underline{2}}$$

ii) $\underline{\underline{0}}$

Q3a

6/18

Q3b

4/6

c) $8m^2 - 2m - 21 = 0$
 ~~$(4m+14)(2m-12)$~~ $(4m+14)(2m-12)$ ✗ 0

Q3c

0/4

$w^2 + 13w + 40 = 0$
 $(w \quad)(w \quad)$ ✗ 0

d) $6x^2 - 8x - 30 = 0$

Q3d

1/4

$A = 6$ ✓
 $B = -8$ ✓
 $C = -30$ ✓

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$
 ✓ 1

$x = 2.80$ or $x = -1.46$ show your working out